## Appendix A: Integrated model

Aleutian Islands Golden King Crab (Lithodes aequispinus) Stock Assessment Model
Development- East of $174^{\circ} \mathrm{W}$ (EAG) and west of $174^{\circ} \mathrm{W}$ (WAG) Aleutian Island stocks

## Basic population dynamics

The annual [male] abundances by size are modeled using the equation:

$$
\begin{equation*}
N_{t+1, j}=\sum_{i=1}^{j}\left[N_{t, i} e^{-M}-\left(\hat{C}_{t, i}+\widehat{D}_{t, i}+\widehat{\operatorname{Tr}}_{t, i}\right) e^{\left(y_{t}-1\right) M}\right] X_{i, j}+R_{t+1, j} \tag{A.1}
\end{equation*}
$$

where $N_{t, i}$ is the number of [male] crab in length class $i$ on 1 July (start of fishing year) of year $t ; \hat{C}_{t, i}, \hat{D}_{t, i}$, and $\widehat{T} r_{t, i}$ are respectively the predicted fishery retained, pot fishery discard dead, and groundfish fishery discard dead catches in length class $i$ during year $t$; $\widehat{D}_{t, i}$ is estimated from the intermediate total ( $\widehat{T}_{t, i}$ temp $)$ catch and the retained ( $\hat{C}_{t, i}$ ) catch by Equation A.2c. $X_{i, j}$ is the probability of length-class $i$ growing into length-class $j$ during the year; $y_{t}$ is elapsed time period from 1 July to the mid -point of fishing period in year $t ; M$ is instantaneous rate of natural mortality; and $R_{t+1, j}$ recruitment to length class $j$ in year $t+1$.

The catches are predicted using the equations

$$
\begin{align*}
& \hat{T}_{t, j, t e m p}=\frac{F_{t} s_{t, j}^{T}}{Z_{t, j}} N_{t, j} e^{-y_{t} M}\left(1-e^{-Z_{t, j}}\right)  \tag{A.2a}\\
& \hat{C}_{t, j}=\frac{F_{t} s_{t, j}^{T} s_{t, j}^{r}}{z_{t, j}} N_{t, j} e^{-y_{t} M}\left(1-e^{-Z_{t, j}}\right)  \tag{A.2b}\\
& \widehat{D}_{t, j}=0.2\left(\widehat{T}_{t, j, t e m p}-\hat{C}_{t, j}\right)  \tag{A.2c}\\
& \widehat{\operatorname{Tr}}_{t, j}=0.65 \frac{F_{t}^{T r} s_{j}^{T r}}{Z_{t, j}} N_{t, j} e^{-y_{t} M}\left(1-e^{-Z_{t, j}}\right)  \tag{A.2d}\\
& \widehat{T}_{t, j}=\hat{C}_{t, j}+\widehat{D}_{t, j} \tag{A.2e}
\end{align*}
$$

where $Z_{t, j}$ is total fishery-related mortality on animals in length-class $j$ during year $t$ :

$$
\begin{equation*}
Z_{t, j}=F_{t} s_{t, j}^{T} s_{t, j}^{r}+0.2 F_{t} s_{t, j}^{T}\left(1-s_{t, j}^{r}\right)+0.65 F_{t}^{T r} s_{j}^{T r} \tag{A.3}
\end{equation*}
$$

$F_{t}$ is the full selection fishing mortality in the pot fishery, $F_{t}^{T r}$ is the full selection fishing mortality in the trawl fishery, $s_{t, j}^{T}$ is the total selectivity for animals in length-class $j$ by the pot fishery during year $t, s_{j}^{T r}$ is the selectivity for animals in length-class $j$ by the trawl
fishery, $s_{t, j}^{r}$ is the probability of retention for animals in length-class $j$ by the pot fishery during year t . Pot bycatch mortality of 0.2 and groundfish bycatch mortality of 0.65 (average of trawl ( 0.8 ) and fish pot ( 0.5 ) mortality) were assumed.

The initial conditions are computed as the equilibrium initial condition using the following relations:

The equilibrium stock abundance is
$\underline{\mathrm{N}}=\mathbf{X} . \mathbf{S} \cdot \underline{\mathrm{N}}+\underline{\mathrm{R}}$
The equilibrium abundance in $1960, \underline{\mathbf{N}}_{1960}$, is
$\underline{N}_{1960}=(\mathbf{I}-\mathbf{X S})^{-1} \underline{R}$
where $\mathbf{X}$ is the growth matrix, $\mathbf{S}$ is a matrix with diagonal elements given by $e^{-M}, \mathbf{I}$ is the identity matrix, and $\underline{R}$ is the product of average recruitment and relative proportion of total recruitment to each size-class.

We used the mean number of recruits from 1987 to 2012 in equation (A.5) to obtain the equilibrium solution under only natural mortality in year 1960, and then projected the equilibrium abundance under natural mortality with recruitment estimated for each year after 1960 up to 1985 with removal of retained catches during 1981/82 to 1984/85.

## Growth Matrix

The growth matrix $\mathbf{X}$ is modeled as follows:

$$
X_{i, j}= \begin{cases}0 & \text { if } j<i  \tag{A.6}\\ P_{i, j}+\left(1-m_{i}\right) & \text { if } j=i \\ P_{i, j} & \text { if } j>i\end{cases}
$$

where:
$P_{i, j}=m_{i}\left\{\begin{array}{lr}\int_{-\infty}^{j_{2}-L_{i}} N\left(x \mid \mu_{i}, \sigma^{2}\right) d x & \text { if } j=i \\ \int_{j_{1}-L_{i}}^{j_{2}-L_{i}} N\left(x \mid \mu_{i}, \sigma^{2}\right) d x & \text { if } i<j<n, \\ \int_{j_{1}-L_{i}}^{\infty} N\left(x \mid \mu_{i}, \sigma^{2}\right) d x & \text { if } i=n\end{array}\right.$

$$
N\left(x \mid \mu_{i}, \sigma^{2}\right)=\frac{1}{\sqrt{2 \pi \sigma^{2}}} e^{-\left(\frac{x-\mu_{i}}{\sqrt{2} \sigma}\right)^{2}}, \text { and }
$$

$\mu_{\mathrm{i}}$ is the mean growth increment for crabs in size-class $i$ :
$\mu_{\mathrm{i}}=\omega_{1}+\omega_{2} * \bar{L}_{\mathrm{i}}$.
$\omega_{1}, \omega_{2}, \quad$ and $\sigma$ are estimable parameters, and $j_{1}$ and $j_{2}$ are the lower and upper limits of the receiving length-class $j$ (in mm CL ), and $\bar{L}_{\mathrm{i}}$ is the mid-point of the contributing length interval $i$. The quantity $m_{i}$ is the molt probability for size-class $i$ :
$\mathrm{m}_{\mathrm{i}}=\frac{1}{1+\mathrm{e}^{\mathrm{c}\left(\mathrm{f}_{\mathrm{i}}-\mathrm{d}\right)}}$
where $c$ and $d$ are parameters.

## Selectivity and retention

a) Selectivity and retention are both assumed to be logistic functions of length. Selectivity depends on the fishing period for the pot fishery:
$S_{i}=\frac{1}{1+e^{\left[-\ln (19) \frac{\tau_{i}-\theta_{50}}{\left.\theta_{95}-\theta_{50}\right]}\right.}}$
where $\theta_{95}$ and $\theta_{50}$ are the parameters of the selectivity/ retention pattern (Mark Maunder, unpublished generic crab model). In the program, we re-parameterized the denominator $\left(\theta_{95}-\theta_{50}\right)$ to $\log ($ delta $\theta)$ so that the difference is always positive.

## Maturity

Maturity is assumed to be a logistic function of length formulated similar to Eq (A.9),

$$
\begin{equation*}
\text { Mat }_{i}=\frac{1}{1+e^{\left[-\ln (19) \frac{\tau_{i}-\text { mat }_{50}}{\text { mat }_{95}-\text { mat }_{50}}\right]}} \tag{A.10}
\end{equation*}
$$

where mat $_{95}$ and mat ${ }_{50}$ are the parameters of the maturity curve. In the program, we reparameterized the denominator (mat ${ }_{95}-$ mat $_{50}$ ) to $\log ($ delta_mat) so that the difference is always positive.

## Recruitment

Recruitment to length-class $i$ during year $t$ is modeled as $R_{t, i}=\bar{R} e^{\epsilon_{i}} \Omega_{i}$ where $\Omega_{i}$ is a normalized gamma function
$\operatorname{gamma}\left(x \mid \alpha_{r}, \beta_{r}\right)=\frac{x^{\alpha_{r}-1} e^{\frac{x}{\beta_{r}}}}{\beta_{r}{ }^{\alpha_{r}} \Gamma_{\left(\alpha_{r}\right)}}$
with $\alpha_{r}$ and $\beta_{r}$ (restricted to the first six length classes).

## Parameter estimation

Table A1 lists the parameters of the model indicating which are estimated and which are pre-specified. The objective function includes contributions related to the fit of the model to the available data and penalties (priors on the various parameters).

Tables A2 lists parameter values (with the corresponding coefficient of variations in parentheses) used to weight the components of the objective functions for EAG and WAG.

## Likelihood components

## Catches

The contribution of the catch data (retained, total, and groundfish discarded) to the objective function is given by:

$$
\begin{align*}
& L L_{r}^{\text {catch }}=\lambda_{r} \sum_{t}\left\{\ell \operatorname{n}\left(\sum_{j} \hat{C}_{t, j} w_{j}+c\right)-\ell \operatorname{n}\left(\sum_{j} C_{t, j} w_{j}+c\right)\right\}^{2}  \tag{A.12a}\\
& L L_{T}^{\text {catch }}=\lambda_{T} \sum_{t}\left\{\ln \left(\sum_{j} \hat{T}_{t, j} w_{j}+c\right)-\ln \left(\sum_{j} T_{t, j} w_{j}+c\right)\right\}^{2}  \tag{A.12b}\\
& L L_{G D}^{\text {catch }}=\lambda_{G D} \sum_{t}\left\{\ln \left(\sum_{j} \widehat{T r}_{t, j} w_{j}+c\right)-\ln \left(\sum_{j} T r_{t, j} w_{j}+c\right)\right\}^{2} \tag{A.12c}
\end{align*}
$$

where $\lambda_{r}, \lambda_{T}$, and $\lambda_{G D}$ are weights assigned to likelihood components for the retained, pot total, and groundfish discard catches; $w_{j}$ is the average mass of a crab is length-class $j$; $C_{t, j}, T_{t, j}$, and $T r_{t, j}$ are, respectively, the observed numbers of crab in size class $j$ for retained, pot total, and groundfish fishery discarded crab during year $t$, and $c$ is a small constant value. We assumed $c=0.001$.
An additional retained catch likelihood (using Equation A.12a without w) for the retained catch in number of crabs during 1981/82 to 1984/85 was also considered in all scenarios.

## Catch-rate indices

The catch-rate indices are assumed to be lognormally distributed about the model prediction. Account is taken of variation in addition to that related to sampling variation:

$$
\begin{equation*}
L L_{r}^{C P U E}=\lambda_{r, C P U E}\left\{0.5 \sum_{t} \ln \left[2 \pi\left(\sigma_{r, t}^{2}+\sigma_{e}^{2}\right)\right]+\sum_{t} \frac{\left(\ln \left(C P U E_{t}^{r}+c\right)-\ln \left(C \widehat{P U E}_{t}^{r}+c\right)\right)^{2}}{2\left(\sigma_{r, t}^{2}+\sigma_{e}^{2}\right)}\right\} \tag{A.13}
\end{equation*}
$$

where $C P U E_{t}^{r}$ is the standardized retain catch-rate index for year $t, \sigma_{r, t}$ is standard error of the logarithm of $C P U E_{t}^{r}$, and $C \widehat{P U E}_{t}^{r}$ is the model-estimate of $C P U E_{t}^{r}$ :

$$
\begin{equation*}
\widehat{C P U E}{ }_{t}^{r}=q_{k} \sum_{j} S_{j}^{T} S_{j}^{r}\left(N_{t, j}-0.5\left[\widehat{C_{t, j}}+\widehat{D_{t, j}}+\widehat{\operatorname{Tr}_{t, j}}\right]\right) e^{-y_{t} M} \tag{A.14}
\end{equation*}
$$

in which $q_{k}$ is the catchability coefficient during the $k$-th time period (e.g., pre- and postrationalization time periods), $\sigma_{e}$ is the extent of over-dispersion, $c$ is a small constant to prevent zero values (we assumed $\mathrm{c}=0.001$ ), and $\lambda_{r, C P U E}$ is the weight assigned to the catch-rate data. We used the same likelihood formula (A.14) for fish ticket retained catch rate indices for scenario 3 model.

Following Burnham et al. (1987), we computed the $\ln (C P U E)$ variance by:

$$
\begin{equation*}
\sigma_{r, t}^{2}=\ln \left(1+C V_{r, t}^{2}\right) \tag{A.15}
\end{equation*}
$$

## Length-composition data

The length-composition data are included in the likelihood function using the robust normal for proportions likelihood, i.e., generically:
$L L_{r}^{L F}=0.5 \sum_{t} \sum_{j} \ln \left(2 \pi \sigma_{t, j}^{2}\right)-\sum_{t} \sum_{j} \ln \left[\exp \left(-\frac{\left(P_{t, j}-\hat{P}_{t, j}\right)^{2}}{2 \sigma_{t, j}^{2}}\right)+0.01\right]$
where $P_{t, j}$ is the observed proportion of crabs in length-class $j$ in the catch during year $t$, $\hat{P}_{t, j}$ is the model-estimate corresponding to $P_{t, j}$, i.e.:

$$
\begin{gather*}
\hat{L}_{t, j}^{r}=\frac{\hat{C}_{t, j}}{\sum_{j}^{n} \hat{C}_{t, j}} \\
\hat{L}_{t, j}^{T}=\frac{\widehat{T}_{t, j}}{\sum_{j}^{n} \hat{T}_{t, j}} \\
\hat{L}_{t, j}^{G F}=\frac{\widehat{\operatorname{Tr}}_{t, j}}{\sum_{j}^{n} \widehat{T r}_{t, j}} \tag{A.17}
\end{gather*}
$$

$\sigma_{t, j}^{2}$ is the variance of $P_{t, j}$ :

$$
\begin{equation*}
\sigma_{t, j}^{2}=\left[\left(1-P_{t, j}\right) P_{t, j}+\frac{0.1}{n}\right] / S_{t} \tag{A.18}
\end{equation*}
$$

and $S_{t}$ is the effective sample size for year $t$ and $n$ is the number of size classes.

Note: The likelihood calculation for retained length composition starts from length-class 6 (mid length 128 mm CL ) because the length-classes 1 to 5 mostly contain zero data.

## Tagging data

Let $V_{j, t, y}$ be the number of males that were released in year $t$ that were in length-class $j$ when they were released and were recaptured after $y$ years, and $\tilde{V}_{j, t, y}$ be the vector of recaptures by length-class from the males that were released in year $t$ that were in lengthclass $j$ when they were released and were recaptured after $y$ years. The multinomial likelihood of the tagging data is then:

$$
\begin{equation*}
\ln L=\lambda_{y, t a g} \sum_{j} \sum_{t} \sum_{y} \sum_{i} \rho_{j, t, y, i} \ln \hat{\rho}_{j, t, y, i} \tag{A.19}
\end{equation*}
$$

where $\lambda_{y, \operatorname{tag}}$ is the weight assigned to the tagging data for recapture year $y, \hat{\rho}_{j, t, y, i}$ is the proportion in length-class $i$ of the recaptures of males which were released during year $t$ that were in length-class $j$ when they were released and were recaptured after $y$ years:

$$
\begin{equation*}
\underline{\hat{\rho}}_{j, t, y} \propto \underline{s}^{T}[\mathbf{X}]^{y} \underline{\Omega}^{(j)} \tag{A.20}
\end{equation*}
$$

where $\underline{\Omega}^{(j)}$ is a vector with $V_{j, t, y}$ at element $j$ and 0 otherwise, $\mathbf{X}$ is the growth matrix, and $s^{T}$ is the total selectivity vector (Punt et al. 1997).

This likelihood function is predicted on the assumption that all recaptures are in the pot fishery and the reporting rate is independent of the size of crab. The expected number of recaptures in length-class $l$ is given by:

$$
\begin{equation*}
r_{l}=\sum_{t} \sum_{j} \frac{s_{l}\left[\mathbf{X}^{t}\right]_{j, l}}{\sum_{l^{\prime}} s_{l}\left[\mathbf{X}^{t}\right]_{j, l^{\prime}}} \sum_{k} V_{j, k, t} \tag{A.21}
\end{equation*}
$$

The last term, $\sum_{k} V_{j, k, t}$, is the number of recaptured male crab that were released in
length-class $j$ after t time-steps. The term $\sum_{j} \frac{s_{l}\left[\mathbf{X}^{t}\right]_{j, l}}{\sum_{l^{\prime}} s_{l^{\prime}}\left[\mathbf{X}^{t}\right]_{j, l^{\prime}}} \sum_{k} V_{j, k, t}$ is the predicted number of animals recaptured in length-class $l$ that were at liberty for t time-steps.

Maturity proportion likelihood
$L L_{\text {maturity }}=\lambda_{\text {maturity }} \sum_{j}\left(\hat{P}_{j}-P_{j}\right)^{2}$
where $\lambda_{\text {msturity }}$ is the weight assigned to the maturity likelihood component; $P_{j}$ and $\hat{P}_{j}$ are the observed and expected maturity proportions respectively of male crab in size class $j$. We assumed $\lambda_{\text {maturity }}=1.0$.

## Penalties

Penalties are imposed on the deviations of annual pot fishing mortality about mean pot fishing mortality, annual trawl fishing mortality about mean trawl fishing mortality, recruitment about mean recruitment, and the posfunction (fpen):

$$
\begin{align*}
P_{1} & =\lambda_{F} \sum_{t}\left(\ell \mathrm{n} F_{t}-\ell \mathrm{n} \bar{F}\right)^{2}  \tag{A.23}\\
P_{2} & =\lambda_{F^{T r}} \sum_{t}\left(\ell \mathrm{n} F_{t}^{T r}-\ell \mathrm{n} \bar{F}^{T r}\right)^{2}  \tag{A.24}\\
P_{3} & =\lambda_{R} \sum_{t}\left(\ell \mathrm{n} \varepsilon_{t}\right)^{2}  \tag{A.25}\\
P_{5} & =\lambda_{\text {posfn }} * \text { fpen } \tag{A.26}
\end{align*}
$$

## Standardized Residual of Length Composition

$$
\begin{equation*}
\text { Std. } \text { Res }_{t, j}=\frac{P_{t, j}-\widehat{P_{t, j}}}{\sqrt{2 \sigma_{t, j}^{2}}} \tag{A.27}
\end{equation*}
$$

## Output Quantities

Harvest rate

Total pot fishery harvest rate:

$$
\begin{equation*}
\mathrm{E}_{\mathrm{t}}=\frac{\sum_{\mathrm{j}=1}^{\mathrm{n}}\left(\widehat{\mathrm{C}}_{\mathrm{j}, \mathrm{t}}+\widehat{\mathrm{D}}_{\mathrm{j}, \mathrm{t}}\right)}{\sum_{\mathrm{j}=1} \mathrm{~N}_{\mathrm{j}, \mathrm{t}}} \tag{A.28}
\end{equation*}
$$

Exploited legal male biomass at the start of year t :
$L M B_{t}=\sum_{j=\text { legal size }}^{n} s_{j}^{T} s_{j}^{r} N_{j, t} w_{j}$
where $w_{j}$ is the weight of an animal in length-class j .
Mature male biomass on 15 February spawning time (NPFMC 2007) in the following year:
$\mathrm{MMB}_{\mathrm{t}}=\sum_{\mathrm{j}=\text { mature size }}^{\mathrm{n}}\left\{\mathrm{N}_{\mathrm{j}, \mathrm{t}} \mathrm{e}^{-\mathrm{y}^{\prime} \mathrm{M}}-\left(\widehat{\mathrm{C}}_{\mathrm{j}, \mathrm{t}}+\widehat{\mathrm{D}}_{\mathrm{j}, \mathrm{t}}+\widehat{\operatorname{Tr}}_{\mathrm{j}, \mathrm{t}}\right) \mathrm{e}^{\left(\mathrm{yyt}_{\mathrm{t}}-\mathrm{y}^{\prime}\right) \mathrm{M}}\right\} \mathrm{w}_{\mathrm{j}}$
where $y^{\prime}$ is the elapsed time from 1 July to 15 February in the following year.
For estimating the next year limit harvest levels from current year stock abundances, a $\mathrm{F}_{\text {OFL }}$ value is needed. Current crab management plan specifies five different Tier formulas for different stocks depending on the strength of information available for a stock, for computing $\mathrm{F}_{\text {OFL }}$ (NPFMC 2007). For the golden king crab, the following Tier 3 formula is applied to compute $\mathrm{F}_{\mathrm{OFL}}$ :

If,
$\mathrm{MMB}_{\text {current }}>\mathrm{B}_{35 \%}, \mathrm{~F}_{\text {OFL }}=\mathrm{F}_{35 \%}$

$$
\begin{aligned}
& \text { If, } \\
& \mathrm{MMB}_{\text {current }} \leq \mathrm{B}_{35 \%} \text { and } \mathrm{MMB}_{\text {current }}>0.25 \mathrm{~B}_{35 \%}, \\
& \mathrm{~F}_{\mathrm{OFL}}=\mathrm{F}_{35 \%} \frac{\left(\frac{\left(\frac{\mathrm{MMB}_{\text {current }}}{} \mathrm{B}_{35 \%}=\alpha\right)}{(1-\alpha)}\right.}{\text { If, }} \\
& \mathrm{MMB}_{\text {current }} \leq 0.25 \mathrm{~B}_{35 \%} \\
& \mathrm{~F}_{\mathrm{OFL}}=0
\end{aligned}
$$

where $\alpha$ is a parameter, $\mathrm{MMB}_{\text {current }}$ is the mature male biomass in the current year and $\mathrm{B}_{35 \%}$ is the proxy $\mathrm{MMB}_{\mathrm{MSY}}$ for Tier 3 stocks. We assumed $\alpha=0.1$.

Because projected $\mathrm{MMB}_{\mathrm{t}}$ (i.e., $\mathrm{MMB}_{\text {current }}$ ) depends on the intervening retained and discard catch (i.e., $M M B_{t}$ is estimated after the fishery), an iterative procedure is applied using Equations A. 30 and A. 31 with retained and discard catch predicted from Equations A.2b-d. The next year limit harvest catch is estimated using Equations A.2b-d with the estimated $\mathrm{F}_{\mathrm{OFL}}$ value.

## Additional Penalty Functions for Profiles

$M$ estimation:
We used the following penalty function (P6) to estimate $M$ for scenario 0a :
$\mathrm{P}_{6}=\frac{0.5}{\ln \left(1+\mathrm{CV}^{2}\right)}\left[(\ln (\mathrm{M})-\ln (0.18))^{2}\right]$
where a CV of $50 \%$ is assigned to the penalty and $0.18 \mathrm{yr}^{-1}$ is the $M$ value used for king crab stock assessments.
For $M$ profile investigation, we disregarded the $M$ penalty and estimated total and component negative log likelihood values at fixed input $M$ values varied by $\pm 0.30$ proportion of the base scenario estimate.

Mean MMB profile:
If the current_phase $=1$,

$$
\mathrm{P}_{7}=\mathrm{a} 1\left(\text { meanMMB }- \text { meanMMB }^{\text {input }}\right)^{2}
$$

If the current_phase > 1 and the current_phase < = selectivity_phase,

$$
\begin{equation*}
P_{7}=\mathrm{a} 2\left(\text { meanMMB }- \text { meanMMB }^{\text {input }}\right)^{2} \tag{A.33}
\end{equation*}
$$

If the current_phase > selectivity_phase,

$$
P_{7}=\mathrm{a} 3\left(\text { meanMMB }- \text { meanMMB }^{\text {input }}\right)^{2}
$$

where a1, a2, and a3 are weights 0.05 (for EAG) or 0.01 (for WAG), 0.25 (for EAG) or 0.02 (for WAG), and 1.5 (for EAG) or 0.025 (for WAG), respectively. The superscript 'input" refers to a fixed input value. The fixed input values were varied by $\pm 0.25$ proportion of the scenario 1 estimate.

MMB depletion rate profile:
If the current_phase $=1$,

$$
\mathrm{P}_{8}=\mathrm{b} 1\left(\mathrm{MMB}_{\text {depletion }}-\mathrm{MMB}_{\text {depletion }}^{\text {input }}\right)^{2}
$$

If the current_phase > 1 and the current_phase <= selectivity_phase,

$$
\begin{equation*}
\mathrm{P}_{8}=\mathrm{b} 2\left(\mathrm{MMB}_{\text {depletion }}-\mathrm{MMB}_{\text {depletion }}^{\text {input }}\right)^{2} \tag{A.34}
\end{equation*}
$$

If the current_phase > selectivity_phase,

$$
\mathrm{P}_{8}=\mathrm{b} 3\left(\mathrm{MMB}_{\text {depletion }}-\mathrm{MMB}_{\text {depletion }}^{\text {input }}\right)^{2}
$$

Where b1, b2, and b3 are weights $0.05,0.25$, and 15,000 , respectively. The superscript 'input" refers to a fixed input value. $\mathrm{MMB}_{\text {depletion }}=\frac{\mathrm{MMB}_{2015}}{\mathrm{MMB}_{1960}}$. The fixed input values were varied by $\pm 0.25$ proportion of the scenario 1 estimate.

Table A1. Pre-specified and estimated parameters of the population dynamics model

| Parameter | Number of parameters |
| :---: | :---: |
| Initial conditions: |  |
| Length specific equilibrium abundance, $N_{1960, l}$ | 17 (estimated) |
| Fishing mortalities: |  |
| Pot fishery, $F_{t}$ | 1985-2015 (estimated) |
| Mean pot fishery fishing mortality, $\bar{F}$ | 1 (estimated) |
| Groundfish fishery, $F_{t}{ }^{T r}$ | 1989-2015 (the mean F for 1989 to 1994 was used to estimate trawl discards back to 1985 (estimated) |
| Mean groundfish fishery fishing mortality, $\bar{F}^{T r}$ | 1 (estimated) |
| Selectivity and retention: |  |
| Pot fishery total selectivity, $\theta_{50}^{T}$ | 2 or 3 (1985-2004; 2005+) (estimated) |
| Pot fishery total selectivity difference, $\operatorname{delta} \theta^{T}$ | 2 or 3 (1985-2004; 2005+) (estimated) |
| Pot fishery retention, $\theta_{50}^{r}$ | 1 (1985+) (estimated) |
| Pot fishery retention selectivity difference, delta $\theta^{r}$ | 1 (1985+) (estimated) |
| Groundfish fishery selectivity | fixed at 1 for all size-classes |
| Maturity: |  |
| maturity, mat ${ }_{50}$ | 1 (estimated) |
| maturity difference, delta_mat | 1 (estimated) |
| Growth: |  |
| Expected growth increment, $\omega_{1}, \omega_{2}$ | 2 (estimated) |
| Variability in growth increment, $\sigma$ | 1 (estimated) |
| Molt probability (size transition matrix with tag data), $a$ | 1 (estimated) |
| Molt probability (size transition matrix with tag data), $b$ | 1 (estimated) |
| Natural mortality, M | 1 (pre-specified, $0.224 \mathrm{yr}^{-1}$ ) |
| Recruitment: |  |
| Number of recruiting length-classes | 5 (pre-specified) |
| Mean recruit length | 1 (pre-specified, 110 mmCL ) |
| Distribution to length-class, $\beta_{r}$ | 1 (estimated) |
| Median recruitment, $\bar{R}$ | 1 (estimated) |
| Recruitment deviations, $\varepsilon_{t}$ | 56 (1961-2016) (estimated) |
| Fishery catchability, q | 2 (1985-2004; 2005+) or 3 (19851994; 1995-2004; 2005+) (estimated) |
| Additional CPUE indices standard deviation, $\sigma_{e}$ | 1 (estimated) |
| Likelihood weights (coefficient of variation) | Pre-specified, varies by scenario |

Table A2. Specifications for the weights with corresponding coefficient of variations* in parentheses for each scenario for EAG and WAG. select. phase $=$ selectivity phase.


| Table A2 Scenarios 1 to 7 continued. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Groundfish fishing mortality dev, $\lambda_{F^{T r}}$ | Initially 1000, relaxed to 0.001 at phases $\geq$ select. phase | Initially 1000, relaxed to 0.001 at phases $\geq$ select. phase | Initially 1000, relaxed to 0.001 at phases $\geq$ select. phase | Initially 1000, relaxed to 0.001 at phases $\geq$ select. phase | Initially 1000, relaxed to 0.001 at phases $\geq$ select. phase | Initially <br> 1000, relaxed <br> to 0.001 at <br> phases $\geq$ <br> select. phase | Initially 1000, relaxed to 0.001 at phases $\geq$ select. phase |
| Recruitment, $\lambda_{R}$ | 2 (0.533) | 2 | 2 | 2 | 2 | 2 | 2 |
| Posfunction (to keep abundance estimates always positive), $\lambda_{\text {posfn }}$ | 1000 (0.022) | 1000 | 1000 | 1000 | 1000 | 1000 | 1000 |
| Maturity | 1(0.805) | 1 | 1 | 1 | 1 | 1 | 1 |
| Tagging likelihood | EAG individual tag returns | EAG tag data | EAG tag data | EAG tag data | EAG tag data | EAG tag data | EAG tag data |

* Coefficient of Variation, $C V=\sqrt{\exp \left[\frac{1}{2 W}\right]-1}, \quad$ w =weight

Table A2 continued.

| Weight | Value |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Scenario 8 | Scenario 9 | Scenario 10 | Scenario 11 |
| Catch: |  |  |  |  |
| Retained catch. $\lambda_{r}$ | 500 (0.032) | 500 | 500 | 500 |
| Total catch, $\lambda_{T}$ | Number of sampled pots scaled to a max | Number of sampled pots scaled to a max | Number of sampled pots scaled to a max | Number of sampled pots scaled to a max |
|  |  | 250 | 250 | 250 |
| Groundfish bycatch, $\lambda_{G D}$ | 0.2 (3.344) | 0.2 | 0.2 | 0.2 |
| Catch-rate: |  |  |  |  |
| Observer legal size crab catchrate, $\lambda_{r, \text { CPUE }}$ | 1(0.805) | 1 | 1 | 1 |
| Fish ticket retained crab catchrate, $\lambda_{r, \text { CPUE }}$ | 1(0.805) | 1 | 1 | 1 |
| Penalty weights: |  |  |  |  |
| Pot fishing mortality dev, $\lambda_{F}$ | Initially 1000 , relaxed to 0.001 at phases $\geq$ select.phase | Initially 1000 , relaxed to 0.001 at phases $\geq$ select.phase | Initially 1000 , relaxed to 0.001 at phases $\geq$ select. phase | Initially 1000 , relaxed to 0.001 at phases $\geq$ select. phase |
| Trawl fishing mortality dev, $\lambda_{F^{T r}}$ | Initially 1000 , relaxed to 0.001 at phases $\geq$ select. phase | Initially 1000 , relaxed to 0.001 at phases $\geq$ select. phase | Initially 1000 , relaxed to 0.001 at phases $\geq$ select. phase | Initially 1000 , relaxed to 0.001 at phases $\geq$ select. phase |
| Recruitment, $\lambda_{R}$ | $2(0.533)$ | 2 | 2 | 2 |
| Posfunction (to keep abundance estimates always positive), $\lambda_{\text {posfn }}$ | 1000 (0.022) | 1000 | 1000 | 1000 |

Table A2 Scenarios 8 to 11 continued.

| Maturity | $1(0.805)$ | fixed | 1 | fixed |
| :--- | :--- | :--- | :--- | :--- |
| Tagging likelihood | EAG tag data | EAG tag data | EAG tag data | EAG tag data |

